# Generalized Fault Trees: from reliability to security.

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Abstract. Fault Trees (FT) are widespread models in the reliability field, but they lack of modelling power. So, in the literature, several extensions have been proposed and introduced specific new modelling primitives. Attack Trees (AT) have gained acceptance in the field of security. They follow the same notation of standard FT, but they represent the combinations of actions necessary for the success of an attack to a computing system. In this paper, we extend the AT formalism by exploiting the new primitives introduced in specific FT extensions. This leads to more accurate models. The approach is applied to a case study: the AT is exploited to represent the attack mode and compute specific quantitative measures about the system security.

**Keywords:** Attack Trees; Fault Trees; Petri Nets; dynamic gates; repair box; parametric form; simulation; reliability; security.

## 1 INTRODUCTION

Fault Trees (FT) [1] are widespread models in the reliability field and represent how combinations of component failures (called basic events) lead to the system failure (top event). Basic events are Boolean variables whose value turn from false to true when the component fails. The intermediate events (subsystem failures) and the top event are Boolean variables as well, with the same semantics of basic events, so their value can be determined by means of Boolean gates (AND, OR, etc.). From a FT model, we can obtain the minimal cut sets which are the minimal sets of component failures (basic events) determining the system failure (top event). If a probability distribution is associated with basic events, the FT allows the computation of several probabilistic measures, such as the system unreliability (the probability that the system is failed at a given time), the probability of minimal cut sets, and importance (sensitivity) indices. The FT modelling power is rather limited, mainly because basic events are assumed to be independent. So, in the literature, several FT extensions have been proposed introducing new modelling capabilities, as described in Sec. 2.

Attack Trees (AT) [2] can be considered the application of FT in the field of security. In other words, an AT follows the same formalism of a FT, but the

goal is representing the combinations of actions (basic events) by an attacker, in order to succeed in compromising a system (top event). AT can be used to both graphically represent the attack mode, and assess the system security: both the qualitative analysis (minimal cut sets detection) and the quantitative analysis (computation of probabilistic measures) can be performed.

AT typically exploit only Boolean gates in order to express the attack mode. So, AT and FT have the same modelling power. In this paper, we propose to include in an AT model all the modelling primitives proposed in specific FT extensions, with the goal of designing more accurate FT models expressing more complex attack modes. In particular, in Sec. 3, we model and evaluate a case study by means of an AT including *Boolean gates, dynamic gates, repair boxes*, and the *parametric form*. The AT model is evaluated by means of Petri Net [1] generation and simulation, with the goal of computing quantitative indices concerning the system security. The case study is taken from [3]; in the current paper, we present the complete model design and evaluation.

# 2 RELATED WORK

**Fault Trees.** One of the ways to improve the reliability of a system, consists of replicating its critical components or subsystems; in these cases, the construction and the analysis of the FT may become quite unpractical because the model will be composed by several identical (large) sub-trees representing the replicated parts. Parametric Fault Trees (PFT) [4] were proposed with the purpose of providing the compact modelling of such parts. Using PFT, identical sub-trees are folded into a single parametric sub-tree, while the identity of each replica is maintained through the possible values of the parameters. Dynamic Fault Trees (DFT) [5] introduced dynamic gates representing several kinds of dependency between events: functional dependencies, dependencies concerning the order of events, and the presence of spare components. Repairable Fault Trees (RFT) [6] introduced a new primitive called repair box representing the presence of a repair process involving a certain set of components, and activated by the occurrence of a specific failure event. In [7,8] the modelling primitives present in FT, PFT, DFT and RFT formalisms have been integrated into a single formalism called Generalized Fault Tree (GFT). So, in a GFT model, we can exploit in a combined way, the compact modelling of redundancies and symmetries, the dependencies between events, the repair of components or subsystems.

Boolean logic Driven Markov Processes (BDMP) [9] are another extension of FT. In particular, BDMP exploit traditional Boolean gates, Markov processes can be associated with basic events, and trigger arcs are used to "activate" a Markov process as a consequence of an event. The elements of the BDMP formalism can model the same dependencies set by dynamic gates in DFT, and other situations such as recovery actions or multi-state components.

Attack Trees. The methodology of AT has become popular and has been applied in several contexts, such as SCADA systems [10, 11]. Defence Trees (DT)

are an extension of AT where defense mechanisms or countermeasures are incorporated. In particular, in [12], they can be represented by basic events, while in [13, 14], they can appear at any level in the DT; in [15], the point of view of the attacker as well as the point of view of the defender can be analysed. Another case of model adaptation from reliability to security is the application of BDMP models to represent and evaluate attacks [16]. In particular, three types of basic event represent specific types of event during the attack.

Petri Nets. Besides AT, Petri Net based models have been applied to security: Attack nets [17] for penetration testing, and Stochastic Activity Networks (SAN) [18] with several purposes [19–22]. In general, AT models are easy to build and very readable, but they lack of modelling power because they can only represent the features that gates can express. Petri Net based models can model more complex events, but they are harder to build, less readable and less intuitive to interpret. A trade-off is the generation of Petri Net models from AT. In this way, the attack can be easily represented as a familiar model like AT, and the corresponding Petri Net can be automatically generated, and possibly edited to include further aspects that AT cannot capture. This approach has been applied in several works: in [23] a standard AT is converted into a Colored Petri Net with the aim of evaluating the model. The same goal is achieved in [24], but resorting to Generalized Stochastic Petri Nets (GSPN) [1]. The Petri Net attack modeling approach (PENET) [25] extends this approach by taking into account also some of the dynamic gates introduced in DFT, such as the *Priority* AND (PAND) gate [5], and exploits Deterministic timed transitions Petri Nets (DTTPN).

The same approach is applied in the current work where the AT model is conform to the GFT formalism providing several advantages:

- we can model the presence of recovery, as in the case of DT.
- All the dynamic gates of DFT are available (PAND, SEQ, WSP, FDEP [5]), instead of a subset;
- The parametric form allows to model in a compact way the contemporary presence of several attackers, while AT typically consider a single attacker. This allows the computation of quantitative measures concerning contemporary attempts of attack (Sec. 3.2).
- The presence of all the modelling primitives introduced in FT, PFT, DFT and RFT makes the AT an higher-level model which is more readable with respect to other dynamic extensions of AT or FT, such as BDMP where the dynamic aspects are "hidden" in the basic events or in the trigger arcs, instead of being explicitly represented by means of specific nodes.
- Modelling primitives taken from different formalisms (FT, PFT, DFT, RFT)
   can be used in a combined way. For instance, a repair box can be applied to
   a parametric subtree containing dynamic gates (Sec. 3.1).

		Mean time to	Occurrence
Event	Description	occurrence $1/\lambda$	rate $\lambda$
v1	occurrence of $v1$		$0.000694 \ h^{-1}$
v2	occurrence of $v2$		$0.000462 \ h^{-1}$
v1REP	recovery of $v1$	$(24 \cdot 10) h$	$0.004166 \ h^{-1}$
v2REP	recovery of $v2$	$(24 \cdot 7) \ h$	$0.005952 \ h^{-1}$
LOGGING_IN	attempt to log-in		$0.020833 \ h^{-1}$
CRACKING	attempt to crack the root password		$0.041666 \ h^{-1}$
GUESSING	attempt to guess the root password	$(24 \cdot 365 \ h)$	$0.000114 \ h^{-1}$
DISCOVERING	removal of a user logged-in	24 h	$0.041666 \ h^{-1}$

**Table 1.** The mean time to occurrence and the corresponding rate for each event in the case study.

# 3 THE CASE STUDY

The case study consists of the acquisition by an attacker, of the root password of a Unix server which is periodically characterized by two vulnerabilities: v1 is the possibility that a not authorized user (attacker) logs-in; v2 is the possibility to crack the root password.

The attack is performed in this way: in the time interval between the occurrence of v1, and the detection and recovery of v1, one or more attackers may try to log-in (event  $LOGGING\_IN$ ). After the detection of v1 (event v1REP), the system administrator may discover and remove the not authorized users logged-in (event DISCOVERING). In order to detect v1, at least one attacker has to be logged-in. The undiscovered attackers keep their presence in the system and may discover the root password in two ways: 1) trying to crack the root password (event CRACKING) during the occurrence of v2; 2) trying to guess the root password (event GUESSING); this operation does not require any vulnerability. Also v2 may be detected and recovered (event v2REP). Both v1 and v2 may occur again after their recovery. The server becomes compromised if at least one attacker succeeds in discovering the root password.

All the events described above may occur if allowed by the current system state and after an interval of time which is a random variable ruled by the negative exponential distribution. Tab. 1 shows the mean time to occurrence of each event, with the corresponding rate  $\lambda$ . Actually the values of  $\lambda$  have been chosen in an arbitrary way. Probability distributions and rates closer to reality might be obtained by means of statistical investigations.

Some events cannot happen before other ones. For example, the attempt to crack the root password (event CRACKING) cannot be performed if the attacker has not succeeded in logging-in and v2 has not occurred. In a similar way, logging-in may be attempted only after the occurrence of v1. These are the temporal dependencies between the events (the symbol  $\prec$  specifies that an event must precede another one):

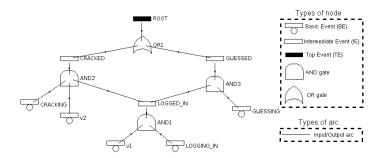


Fig. 1. Standard attack tree model of the case study.

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v1 \prec LOGGING\_IN

v1 \prec v1REP

(LOGGING\_IN \land v2) \prec CRACKING

LOGGING\_IN \prec GUESSING

(LOGGED\_IN \land v1REP) \prec DISCOVERING

v2 \prec v2REP
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Some events, once "enabled", may be repeatable. For instance, while v1 is occurring, one or more attackers may log-in. In a similar way, while v2 is occurring, one or more attackers may discover the root password. The occurrence and the recovery of a vulnerability are instead alternating events.

### 3.1 Model design

Standard AT. A preliminary model of the case study is the standard AT shown in Fig. 1 where only Boolean gates are present (Sec. 1). This model represents the attack mode by a single attacker: the event  $LOGGED\_IN$  represents that the attacker has succeeded in logging-in; it is the output of an AND gate, so it occurs if both its inputs events v1 and  $LOGGING\_IN$  occurs (Tab. 1). The event ROOT models the discovery of the root password and is the output of an OR gate, so it occurs if CRACKED or GUESSED occurs. The event CRACKED represents that the password has been cracked, and occurs if all the events CRACKING, v2 and  $LOGGED\_IN$  have occurred. The event GUESSED occurs if both  $LOGGED\_IN$  and GUESSING have occurred. This model has several limits:

- it considers only a single attacker, while in the case study more attackers may act at the same time.
- It ignores the temporal dependencies between the events specified above; for instance, in the model, LOGGING\_IN may occur at any time, before or after v1; CRACKING may occur before or after LOGGED\_IN or v2.
- It does not take into account the recovery of v1 and v2.

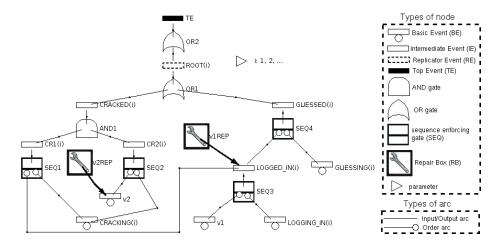


Fig. 2. Attack tree model of the case study, using GFT formalism (the labels of the nodes are explained in Tab. 1).

Such limits can be overcome by the AT shown in Fig. 2. This model contains the modelling primitives collected in the GFT formalism (Sec. 2). The top event (TE), the "root" of the AT, represents the situation where the server is compromised. This happens if at least one attacker discovers the root password.

**Parametric form.** TE is the output of an OR gate connected to the event ROOT(i), with  $i=1,2,\ldots,ROOT(i)$  represents the discovery of the root password by the i-th attacker introduced inside the system. ROOT(i) is actually a replicator event. This means that the sub-tree below ROOT(i) is the compact representation of several sub-trees with the same structure. The identity of each sub-tree is maintained by the possible values of the parameter i which is associated with the events in the sub-tree, with the exception of v1 and v2 which are instead events shared by all the replicated sub-trees. So, each sub-tree folded in the parametric sub-tree, concerns the actions by the i-th attacker (Sec. 2). ROOT(i) is the output of another OR gate, so ROOT(i) happens if the i-th attacker succeeds in cracking (event CRACKED(i)) or guessing the password (event GUESSED(i)).

**Dynamic gates.** We use three Sequence Enforcing (SEQ) gates forcing their input events to occur in a specific order. The output event of this gate corresponds to the last input event in the sequence. The basic event CRACKING(i) (attempt to crack the password by the i-th attacker) is connected as second input, to two SEQ gates. Therefore this event may happen only after the success of the log-in by the i-th attacker (event  $LOGGED_{-}IN(i)$ ) and the vulnerability v2 (basic event v2). In the same way, the attempt to log-in by the i-th attacker

(event  $LOGGING\_IN(i)$ ) may happen only after the vulnerability v1 (basic event v1). Also the event GUESSING(i) (attempt to guess the password by the i-th attacker) is connected to a SEQ gate: such event may happen only after the event  $LOGGED\_IN(i)$ .

Repair box. In an AT, the repair box (Sec. 2) can be used to model the recovery of a vulnerability. In Fig. 2, two repair boxes (Sec. 2) are present: the repair box called v1REP represents the recovery of v1 and the detection of the not authorized users logged in. For this reason, v1REP is connected to the event  $LOGGED\_IN(i)$  due to the sequence of the basic events v1 and  $LOGGING\_IN(i)$ . The repair box v2REP instead, represents only the recovery of the vulnerability v2, so it is connected to the basic event v2. The rates of basic events and repair boxes are the values of  $\lambda$  in Tab. 1.

#### 3.2 Model evaluation

Dependencies are present in the model, due to dynamic gates and repair boxes. Therefore it needs the state space analysis; this means generating all the possible system states and stochastic transitions between states. This can be performed by converting the AT into a *Generalized Stochastic Petri Net* (GSPN) [1]. Then, by exploiting the available GSPN solution techniques, we can generate and the analyze the underlying *Continuous Time Markov Chain* (CTMC) [1]. An alternative to analysis is the GSPN simulation. The AT in Fig. 2 is translated into the GSPN in Fig. 3. Both models have been edited by means of *Draw-Net* [26].

In FT, basic events are repeatable only in case of repair. For instance, a component may fail and then, undergo repair, fail again, and so on. In the AT, a basic event may be repeatable for an undefined number of times, even in absence of recovery. For example, while the system suffers from the vulnerability v1, an attempt to log-in may occur even if another attempt has already been done. As a consequence, any number of attackers may log-in. For this reason, we did not follow the conversion rules defined in [7] because they are oriented to reliability.

The repetitions of basic events leads the dimensions of the state space to become infinite, so the model cannot undergo analysis. A remedy to this problem consists of setting a limit to the number of repetitions of an event. For instance, we could assume that 10 is the highest number of attackers logged-in. This approach reduces the dimensions of the state space, but they still remain relevant, and the model may not be realistic. So, the GSPN obtained from the AT, has been evaluated using simulation instead of analysis. In this way, we avoid to impose limits to the number of event repetitions, and the simulation execution is less expensive than analysis, in terms of computing complexity. We executed 100000 simulation cycles in order to obtain the results described below.

**GSPN.** A GSPN contains places (appearing as circles), immediate transitions (black bars) and timed transitions (white bars). Places contain tokens which are moved by transitions in immediate way or after a random period of time.

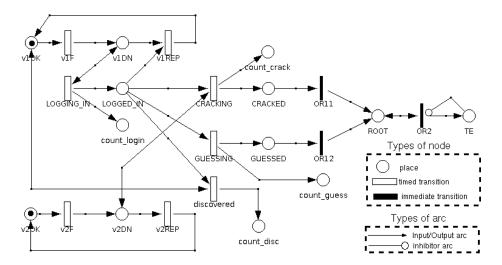


Fig. 3. GSPN model of the case study.

In the GSPN in Fig. 3, the vulnerability v1 is modelled by the places v1OKwhich contains one token in case of absence of v1, and v1DN containing one token in case of presence of v1. The occurrence of v1 is modelled by the transition v1F, while its recovery is modelled by the transition v1REP. The vulnerability v2 is modelled in a similar way. The transition  $LOGGING\_IN$  is enabled by the presence of one token inside the place v1DN, and produces the tokens inside the place LOGGED\_IN corresponding to the number of attackers logged-in. This enables the transition GUESSING moving tokens from the place LOGGED\_IN to the place GUESSED, in order to model the success of password guessing. If marked, the place v1OK enables the transition discovered removing tokens from the place LOGGED\_IN, with the purpose of modelling the removal of attackers from the system. The transition CRACKING is enabled by the contemporary presence of tokens inside the places  $LOGGED_{-}IN$  and v2DN, and moves tokens from LOGGED\_IN to CRACKED, in order to model the success of password cracking. The tokens inside GUESSED or CRACKED are moved into the place ROOT by the transition OR1 or OR2, with the aim of representing that an attacker has obtained the root password. The presence of any quantity of tokens inside ROOT determines the place TE to be marked by one token. This represents that the system is compromised (the place TE corresponds to the top event of the AT).

The rates of timed transitions are the values of  $\lambda$  reported in Tab. 1. With the goal of computing specific indices, further places have been added to the GSPN:  $count\_login$ ,  $count\_disc$ ,  $count\_crack$ ,  $count\_guess$ . They count the number of: successful attempts to log-in, attackers removed from the system, successful attempts to crack the password, successful attempts to guess the password, respectively.

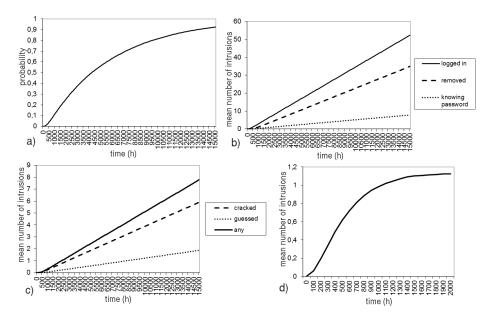


Fig. 4. a) Probability that the system is compromised.

- b) The mean number of: intrusions in the system, discovered intrusions, attackers that have discovered the root password.
- c) The mean number of: attackers that have discovered the root password, by means of password cracking, password guessing, or any of them.
- d) The mean number of undetected attackers that have not discovered yet the root password.

**Results.** Several measures concerning the system security have been computed, as a function of the time varying between 0 and 15000 hours. Fig. 4.a shows the probability that the system has been compromised. This means that at least one attacker has discovered the root password. This measure may be interpreted as the unreliability of the system (Sec. 1), and has been computed as the mean number of tokens present inside the place TE. Since this number can be 0 or 1, its mean provides a probability value. Fig. 4.b shows the mean numbers of intrusions in the system, discovered intrusions, attackers that have discovered the root password by the performance of password cracking or guessing. These measures have been computed as the mean number of tokens inside the places count\_login, count\_disc, ROOT, respectively. Fig. 4.c shows the mean number of attackers that have discovered the root password, by means of password cracking, password guessing, or any method. These measures have been computed as the mean number of tokens inside the places count\_crack, count\_guess, ROOT, respectively. Fig. 4.d shows the mean number of undetected attackers that have not discovered yet the root password (mean number of tokens inside LOGGED\_IN). Such measure reaches a steady value equal to 1.13, after about 3000 hours.

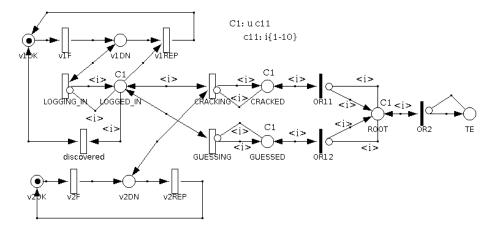


Fig. 5. SWN model of the case study.

**SWN.** An alternative way to solve the AT model in Fig. 2 is the *Stochastic Well-formed Net* (SWN) [27] shown in Fig. 5, instead of GSPN. In the SWN, tokens can be coloured, so the attackers can be distinguished by means of a colour class (C1) associated with the places representing the state of the attack (*LOGGED\_IN*, *CRACKED*, *GUESSED*, *ROOT*). A SWN can be analyzed by generating the corresponding symbolic state space whose size is reduced with respect to the ordinary state space. However, the number of colours in a colour class has to be limited, so the number of attackers has to be limited to a certain amount. SWN can undergo simulation as well.

# 4 CONCLUSIONS

The aim of this paper is transferring our experience about FT extensions, from reliability to security. The GFT formalism defined for reliability evaluation purposes, has been adopted for AT, so that we can model the attack mode by resorting to a single generalized formalism including and integrating Boolean gates, dynamic gates, the parametric form and repair boxes. In this way, the modelling power of AT is improved in a relevant way, so that more accurate models can be designed. The approach has been applied to a case study characterized by recoveries, symmetries and dependencies between events. The current work is a first attempt to use the GFT formalism for AT, so the case study is rather preliminary; however, it serves as proof-of-concept to demonstrate the feasibility of using the GFT formalism, with the consequent improvement of the modelling possibilities. The AT of the case study has been evaluated by conversion into a Petri Net and in particular, a GSPN undergoing simulation. The goal is to avoid the problem of state space explosion, due to the repeatable events.

We believe that the formalism needs further improvements in order to be suitable for the security field. For example, using GFT formalism, the AT model takes into account both the attack mode and the recovery mode. Actually, repair boxes can represent reactive recovery processes. This means that the recovery can be performed only as a consequence of a partial or complete intrusion. The formalism may be extended by taking into account the preventive recovery as well. In this way, preventive countermeasures could be included in the AT model. This was already done in [13, 15], but using only Boolean gates. Moreover, we plan to compute indices which are more security-oriented, with respect to the measures computed in this paper. Importance measures for security are defined in [12, 13], such as Return on Attack (ROA) and Return on Investment (ROI).

Our intention in the future is solving AT models by means of *Dynamic Bayesian Networks* (DBN) [28], already exploited for DFT and RFT analysis. The advantage is the possibility of easily modelling multi-state components and computing predictive, diagnostic, or importance measures conditioned by observations about the system or components state. In the security field, observations may concern the action by intruders, the presence of vulnerabilities or countermeasures. We plan to use AT as an high-level model to represent the attack mode and generate the corresponding DBN.

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